



LAGRANGIAN MECHANICS

# Classical Mechanics

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by  
C. P. Frahm

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**Input Skills:**

1. Vocabulary: Lagrange's equations, Lagrangian, inertial frame (MISN-0-498).

**Output Skills (Knowledge):**

- K1. Vocabulary: Hamiltonian.
- K2. By considering the properties of space and time as seen from an inertial frame derive these conservation laws within the Lagrangian formulation of mechanics: (a) conservation of energy, (b) conservation of linear momentum, (c) conservation of angular momentum.

**Output Skills (Problem Solving):**

- S1. For a given mechanical system determine the Lagrangian and Hamiltonian functions.
- S2. Solve Lagrange's equations of motion to obtain expressions for the generalized coordinates as functions of time.

**External Resources (Required):**

1. J. Marion, *Classical Dynamics*, Academic Press (1988).

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## 1. Introduction

This is a continuation of Unit 498, now with an emphasis on conservation laws and problem solving.

## 2. Procedures

1. Read Sections 7.8 and 7.9 of Marion. You must be prepared to reproduce these arguments, including statements of the conditions under which they are valid.
2. ▷ Work problems 7-5, 7-6, 7-17, 7-18, 7-21, 7-24.
3. (Optional) ▷ Work problems 7-4, 7-19, 7-22.

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